

# Unphysical and Physical Solutions in Many-Body Theories: from Weak to Strong Correlation

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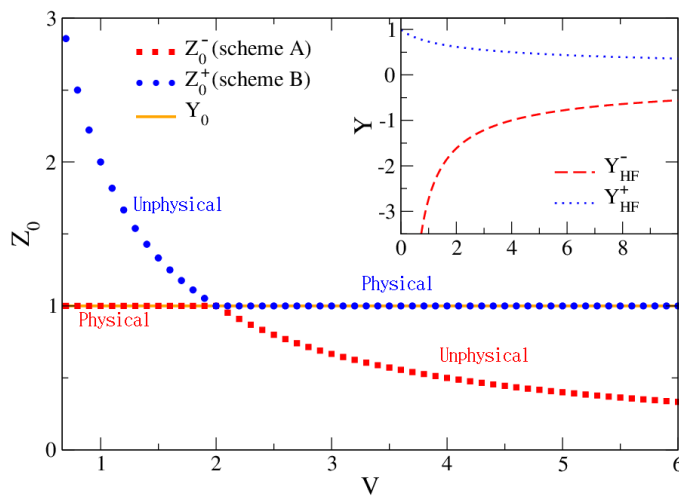
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The noninteracting Green's function  $Z_0$  as a function of the interaction  $V$  obtained in a simple one-point model using two different iteration schemes (**A** and **B**). Squares (red):  $Z_0^-$ , the solution of scheme **A**; circles (blue):  $Z_0^+$ , the solution of scheme **B**; continuous line (orange):  $Y_0$ , the physical noninteracting Green's function

Many-body theory is largely based on self-consistent equations that are constructed in terms of the physical quantity of interest itself, for example the density or the one-body Green's function. Therefore, the calculation of important properties such as total energies or photoemission spectra requires the solution of non-linear equations that have unphysical and physical solutions [1,2]. In this work we show using a simple model in which circumstances one runs into an unphysical solution (see the figure for an example), we illustrate the dramatic consequence that many-body theories become unpredictable, and we indicate how one can overcome this problem [3]. Our findings point out that currently used strategies to develop approximations are only valid in a regime of weak to moderate interaction strength, and that they have to be completely changed in the strong-correlation regime. We propose a new strategy for strong correlation.

[1] G. Lani, P. Romaniello, and L. Reining, *New J. Phys.* 14, 013056 (2012)

[2] J. A. Berger, P. Romaniello, F. Tandetzky, B. S. Mendoza, C. Brouder, and L. Reining, *New J. Phys.* 16, 113025 (2014)

[3] A. Stan, P. Romaniello, S. Rigamonti, L. Reining, and J. A. Berger, *New J. Phys.* 17, 093045 (2015)